Higher Maths - Homework 1

1. The diagram below shows two lines which intersect at the point C .


Show that triangle $A B C$ is right angled at $C$.
F. 2. The diagram below shows the right-angled triangle $O P Q$ and a circle with centre $C(0,5)$ and diameter OS.


Find the equation of the chord RS.
3. The points $R(1,2), S(5,8)$ and $T(11,4)$ lie on the circumference of a circle.


The line with equation $3 x-2 y-12=0$ in the perpendicular bisector of ST.
(a) Find the equation of the perpendicular bisector of RS.

The centre of the circle is the point where the perpendicular bisectors of RS and ST intersect.
(b) Calculate the coordinates of the centre of the circle.
4. The points $\mathrm{A}(3,2), \mathrm{B}(2 a, 12)$ and $\mathrm{C}(a,-1)$ are collinear.

Find the value of the constant $a$.

## Answers to Homework 1 - Straight lines

1. Since $m_{B C} \times m_{A C}=\sqrt{3} \times-\frac{1}{\sqrt{3}}, A C$ and $B C$ are perpendicular and $A B C$ is right-angled at $C$.
2. $y+2 x=10$ (or equivalent)

3(a) $3 y+2 x=21$ (or equivalent) 3 (b) Centre at $(6,3)$
4. $a=\frac{39}{16}$

